

Balance de fuerzas: geostrofia

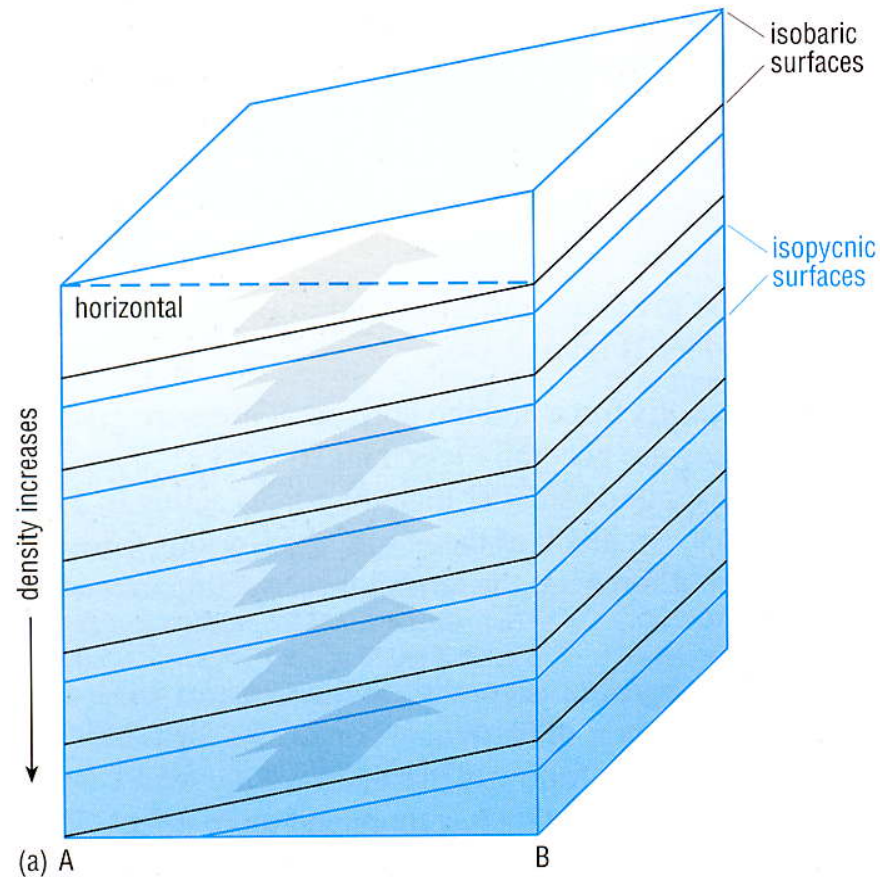
$$-fv = -(1/\rho) \frac{\partial p}{\partial x}$$

$$fu = -(1/\rho) \frac{\partial p}{\partial y}$$

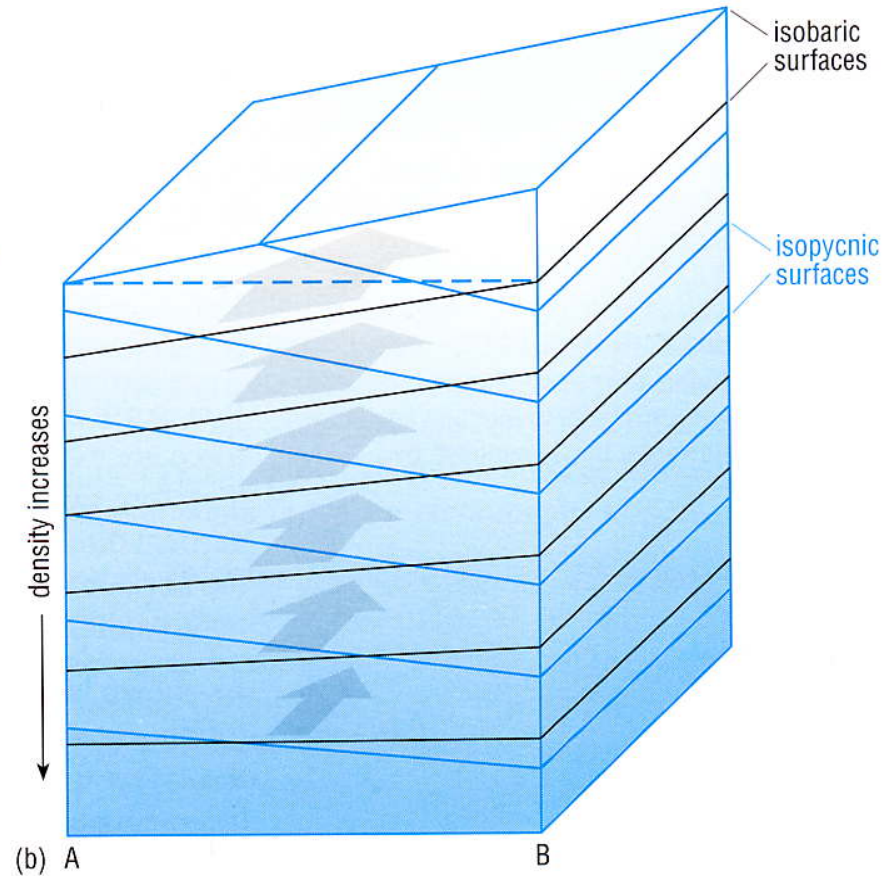
Método para calcular (u,v) a partir de datos de T,S

Condiciones Barotrópicas y Baroclínicas

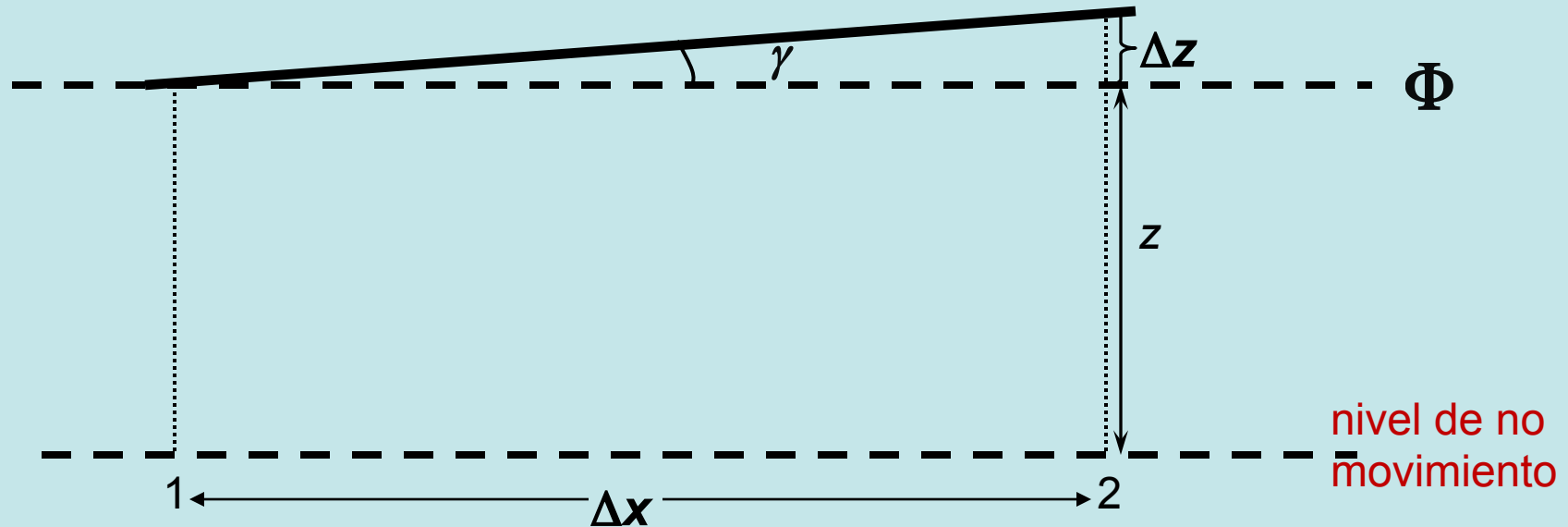
BAROTROPIC CONDITIONS
(ISOBARIC AND ISOPYCNIC SURFACES PARALLEL)



BAROCLINIC CONDITIONS
(ISOBARIC AND ISOPYCNIC SURFACES INCLINED)



Caso barotrópico ($\rho = \text{constante}$)

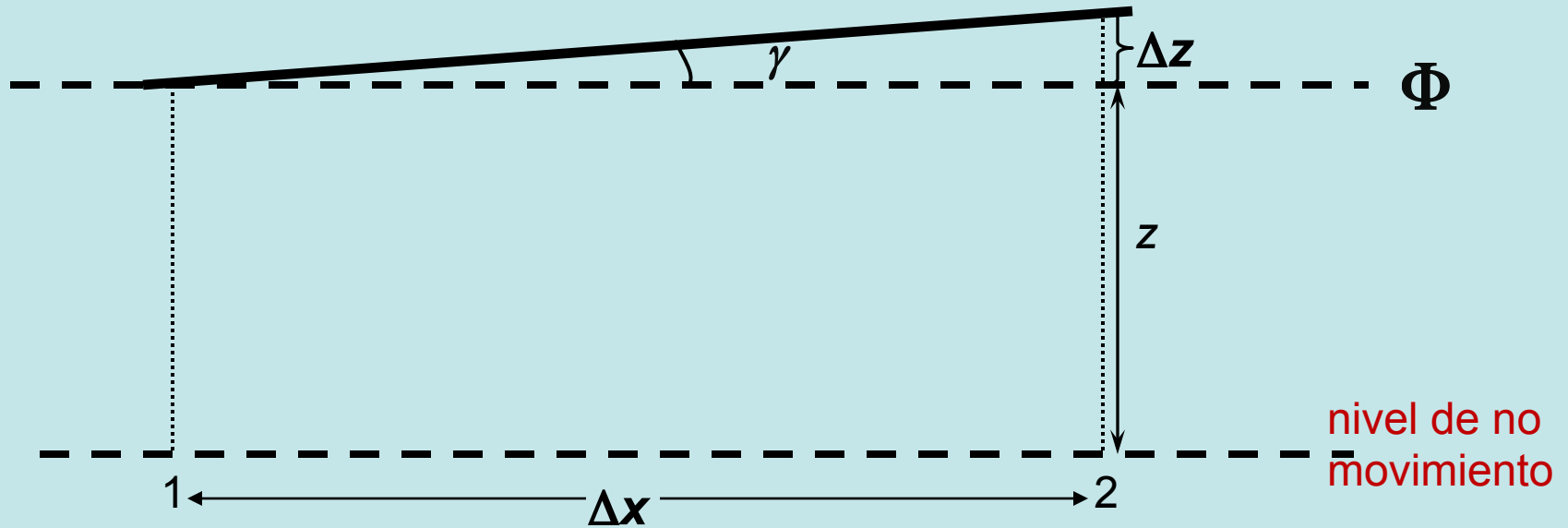


$$P_1 = -\rho g z_1$$

$$P_2 = -\rho g z_2$$

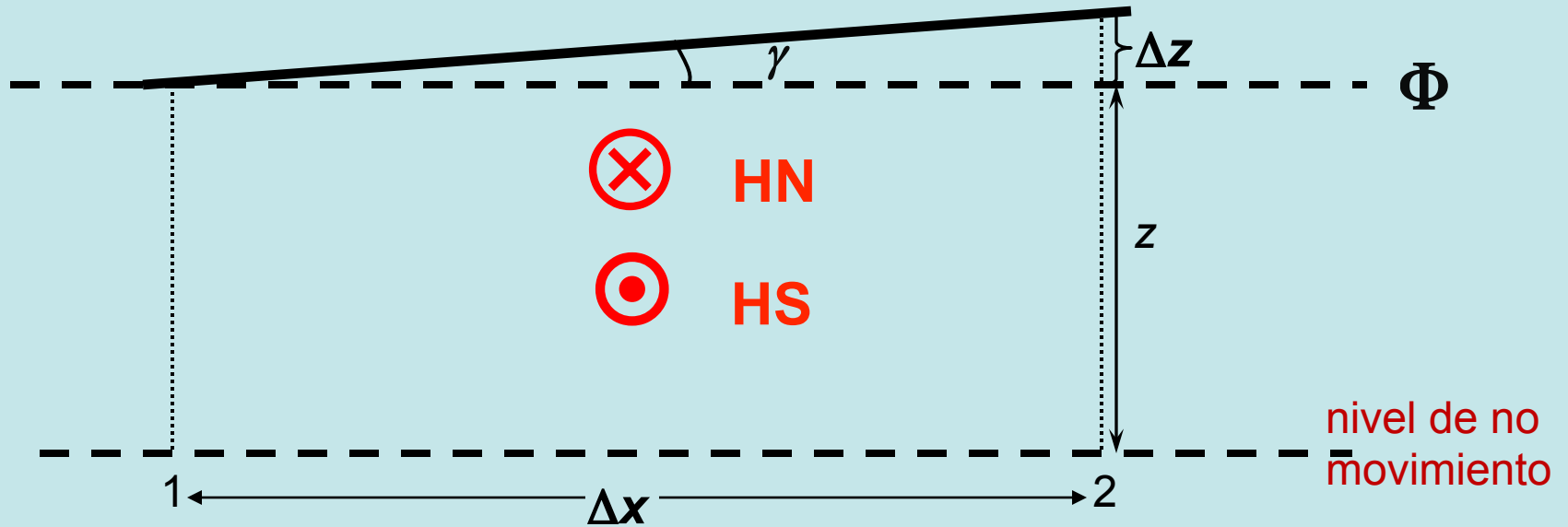
$$\frac{P_2 - P_1}{\Delta x} = \frac{\Delta p}{\Delta x} = -\rho g \frac{\Delta z}{\Delta x}$$

esta es la fuerza del gradiente de presión por unidad de volumen (N/m^3)



La fuerza del gradiente de presión por unidad de masa es:

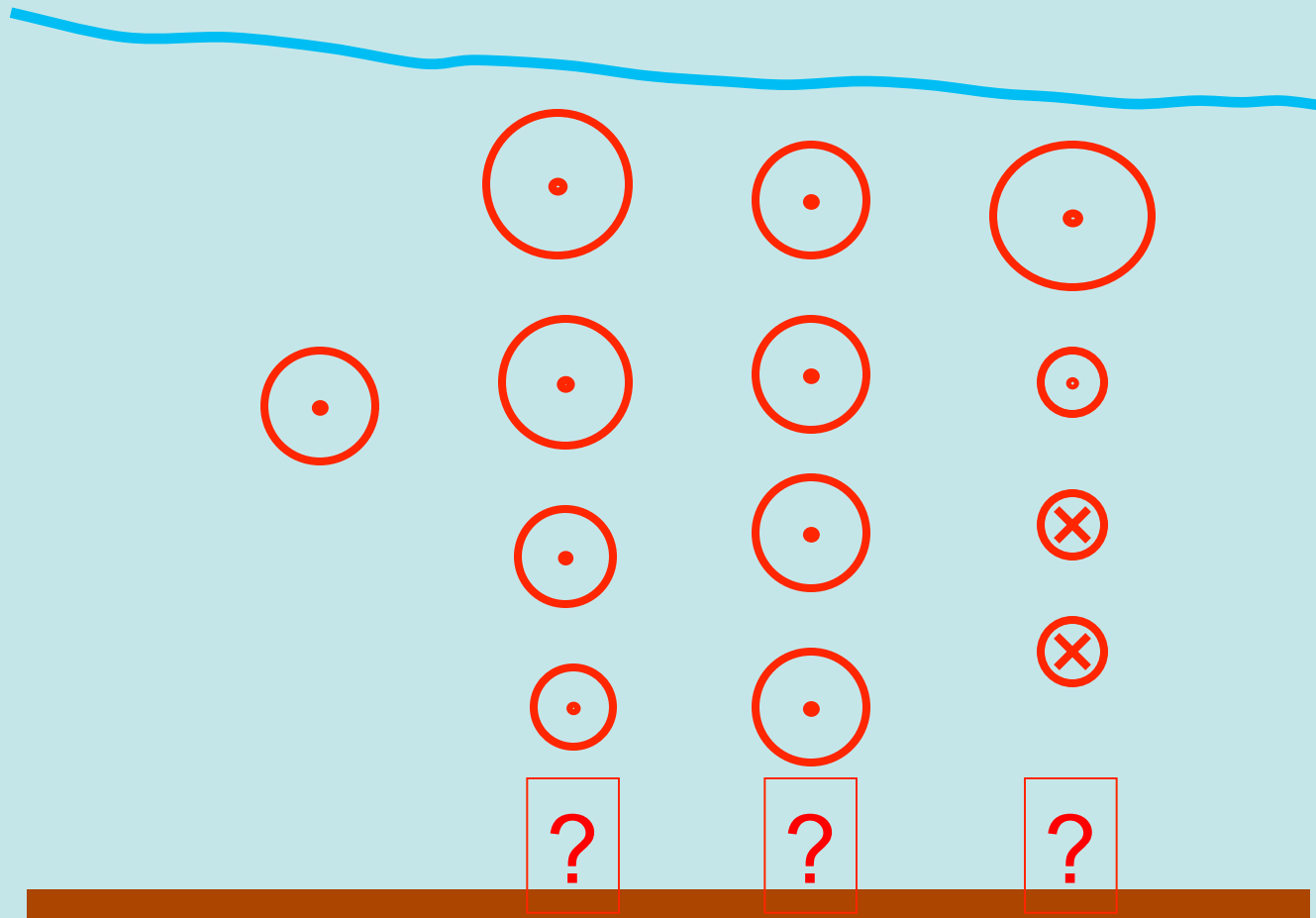
$$\begin{aligned} \frac{F_{GPH}}{\rho} &= \frac{1}{\rho} \left[-\rho g \frac{\Delta z}{\Delta x} \right] \\ &= -g \frac{\Delta z}{\Delta x} \end{aligned}$$



El balance geostrófico está dado por:

$$fU_h = -g \frac{\Delta z}{\Delta x} = -g \tan \gamma$$

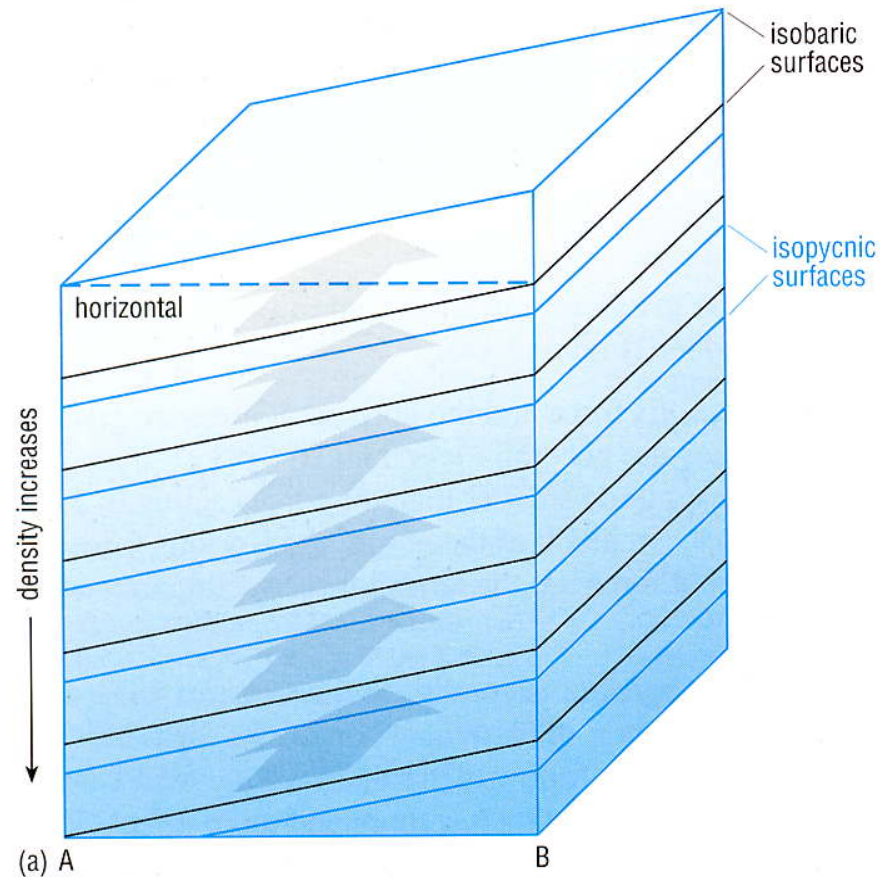
El balance geostrófico ofrece una aproximación para la corriente promedio



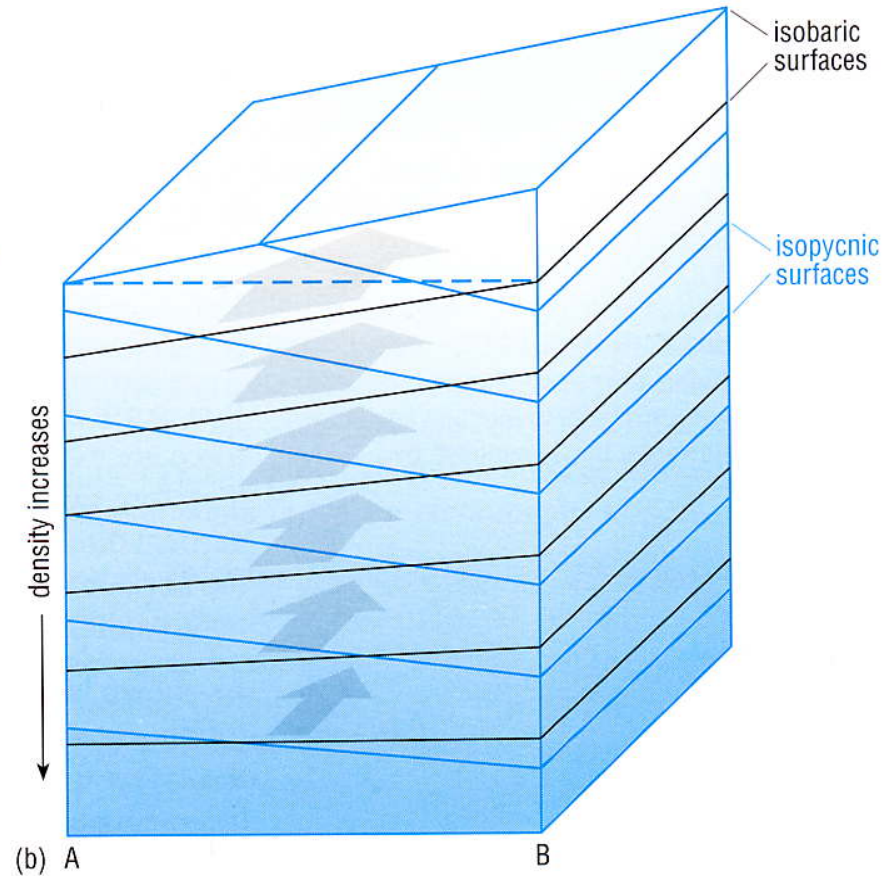
que sucede cuando hay estratificación y la presión depende de densidad ?

Condiciones Barotrópicas y Baroclínicas

BAROTROPIC CONDITIONS
(ISOBARIC AND ISOPYCNIC SURFACES PARALLEL)



BAROCLINIC CONDITIONS
(ISOBARIC AND ISOPYCNIC SURFACES INCLINED)



$$\frac{\partial p}{\partial x} = \rho f v; \quad \frac{\partial p}{\partial y} = -\rho f u; \quad \frac{\partial p}{\partial z} = -\rho g$$

x y z

$$u = -\frac{1}{\rho f} \frac{\partial p}{\partial y}$$

$$v = \frac{1}{\rho f} \frac{\partial p}{\partial x}$$

$$p = p_0 + \int_{-h}^{\eta} g(\varphi, z) \rho(z) dz$$

$$u = -\frac{1}{\rho f} \frac{\partial p}{\partial y} \quad 1$$

$$v = -\frac{1}{\rho f} \frac{\partial p}{\partial x}$$

$$p = p_0 + \int_{-h}^{\eta} g(\varphi, z) \rho(z) dz \quad 2$$

Sustituyendo (2) en (1) se obtiene:

$$u = -\frac{1}{\rho f} \frac{\partial}{\partial y} \int_{-h}^0 g(\varphi, z) \rho(z) dz - \frac{g}{f} \frac{\partial \eta}{\partial y}$$

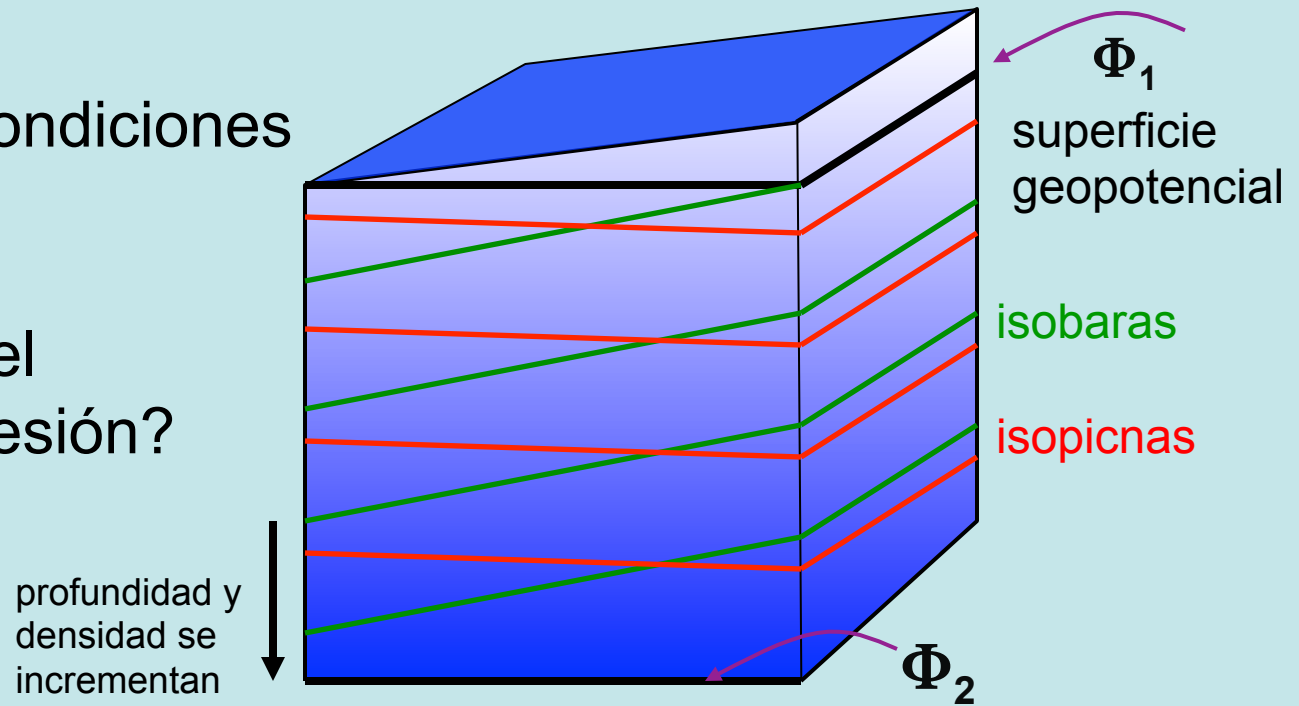
$$u = -\frac{1}{\rho f} \frac{\partial}{\partial y} \int_{-h}^0 g(\varphi, z) \rho(z) dz - u_s$$

$$v = -\frac{1}{\rho f} \frac{\partial}{\partial x} \int_{-h}^0 g(\varphi, z) \rho(z) dz - \frac{g}{f} \frac{\partial \eta}{\partial x}$$

$$v = -\frac{1}{\rho f} \frac{\partial}{\partial x} \int_{-h}^0 g(\varphi, z) \rho(z) dz - v_s$$

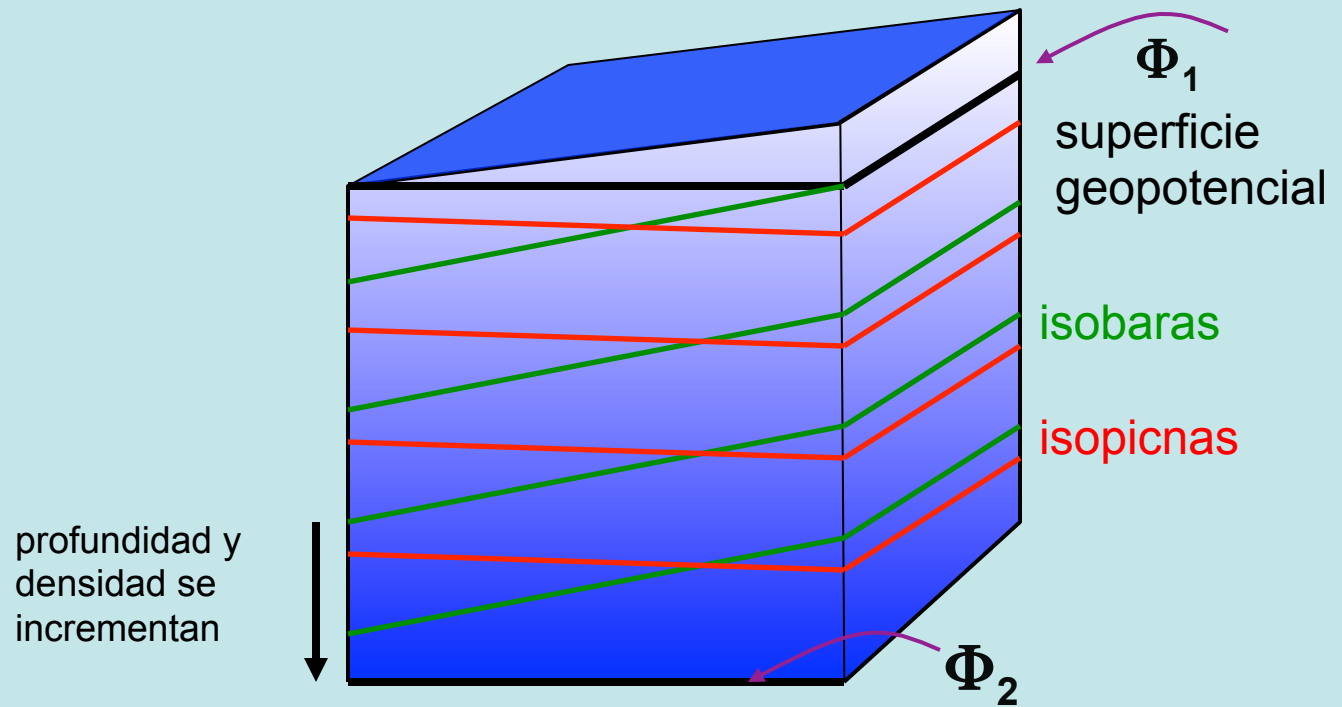
Diagrama de Condiciones Baroclínicas

Como se mide el gradiente de presión?



Definiciones:

Distancia Geopotencial – es la distancia entre dos superficies isobáricas localizadas en z_1 y z_2



El trabajo que se requiere para llevar un volumen de agua con masa ***M*** una distancia ***dz*** en contra de la fuerza de gravedad es $Mgdz$

El cambio de geopotencial $d\Phi$ es la energía potencial por unidad de masa que gana ese volumen de agua, o:

$$d\Phi = g dz \left(J/kg = m^2/s^2 \right) = -\alpha dp$$

$$d\Phi = g dz = -\alpha dp$$

Es necesario calcular $d\Phi$ entre z_1 y z_2 para calcular los gradientes de presión baroclínicos

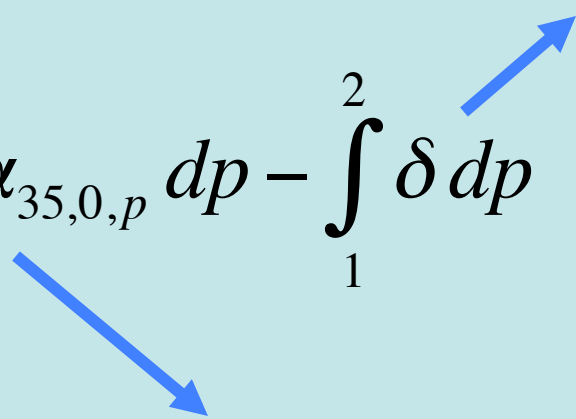
$$\int_1^2 d\Phi = \int_1^2 g dz = \int_1^2 \frac{dp}{\rho} = \int_1^2 \alpha dp$$

Con: $\frac{1}{\rho} = \alpha = \alpha_{35,0,p} + \delta$

$$\int_1^2 d\Phi = \int_1^2 g dz = \int_1^2 \frac{dp}{\rho} = \int_1^2 \alpha dp$$

con $\alpha = \alpha_{35,0,p} + \delta$

anomalía
geopotencial

$$\Phi_2 - \Phi_1 = g(z_2 - z_1) = \int_1^2 \alpha_{35,0,p} dp - \int_1^2 \delta dp$$


Distancia geopotencial
entre z_1 y z_2 donde las
presiones son p_1 y p_2

$\Delta\Phi_{std}$

distancia geopotencial estándar

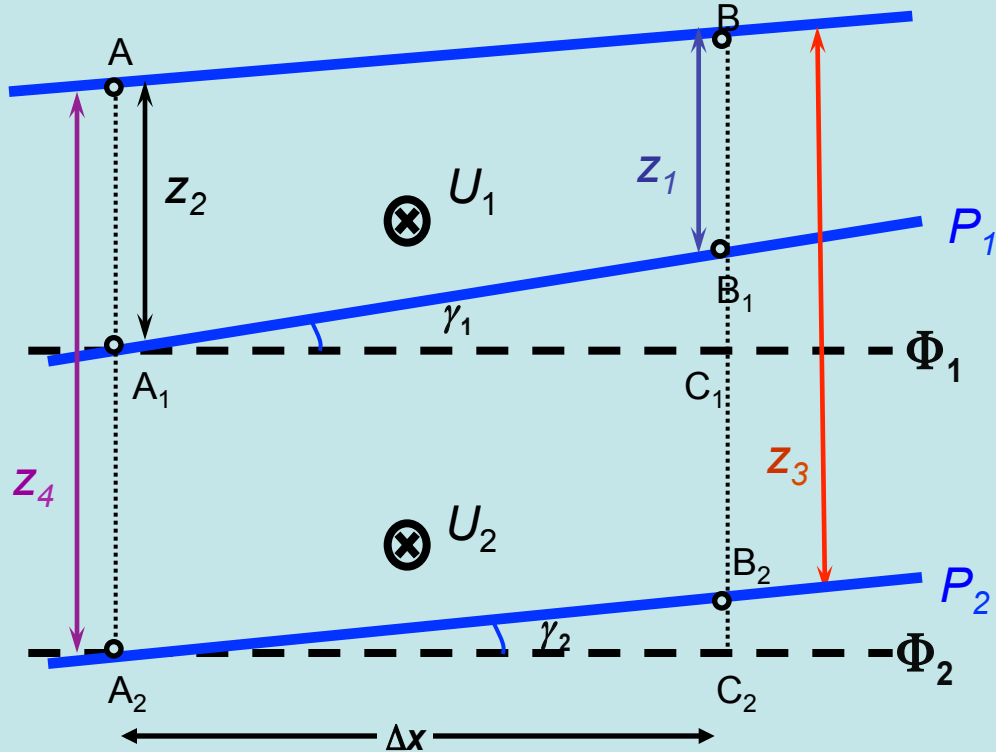
$$\Phi_2 - \Phi_1 = g(z_2 - z_1) = \int_1^2 \alpha_{35,0,p} dp - \int_1^2 \delta dp$$

Unidades son m^2 / s^2 o energía por unidad de masa (J/kg)

si $z_2 - z_1 = 1 \text{ m} \Rightarrow \Phi_2 - \Phi_1 = 9.8 \text{ J/kg} \approx 1 \text{ m dinámico}$

$$= 10 \text{ J/kg} = 10 \text{ m}^2/\text{s}^2$$

La **Topografía Dinámica** se refiere a
Distancias Geopotenciales



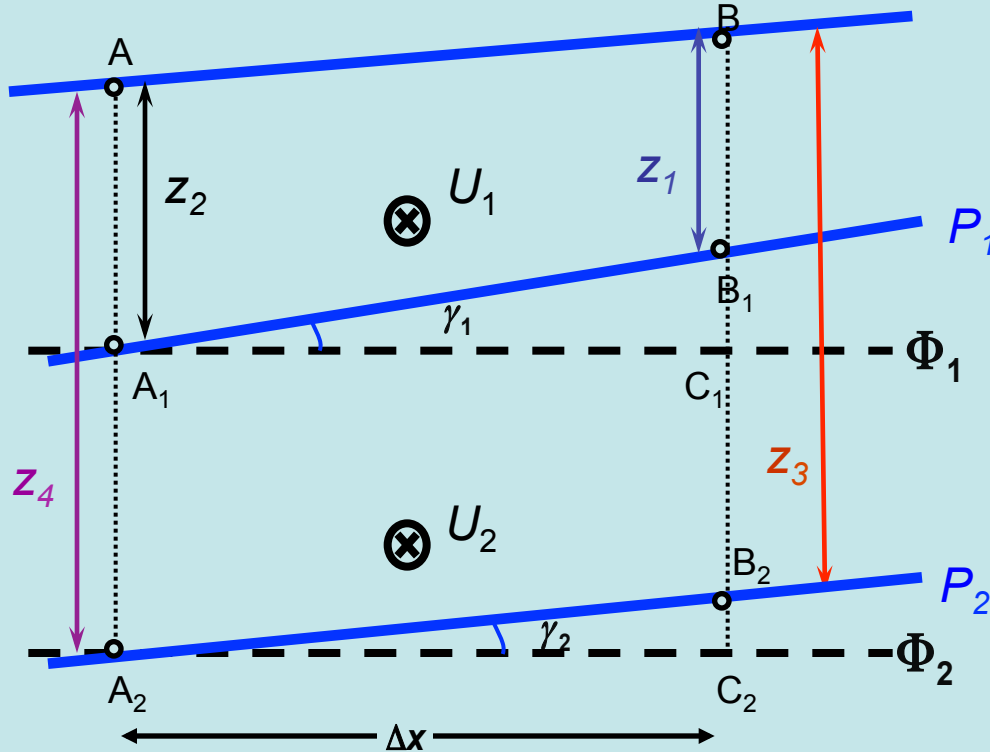
$$fU_1 = g \tan g_1$$

$$fU_2 = g \tan \gamma_2$$

$$f(U_1 - U_2) = g(\tan \gamma_1 - \tan \gamma_2)$$

$$f(U_1 - U_2) = g \left[\frac{B_1 C_1}{A_1 C_1} - \frac{B_2 C_2}{A_2 C_2} \right] = \frac{g}{\Delta x} [B_1 C_1 - B_2 C_2]$$

$$= \frac{g}{\Delta x} [B_1 B_2 - C_1 C_2] = \frac{g}{\Delta x} [B_1 B_2 - A_1 A_2]$$



$$fU_1 = g \tan \gamma_1$$

$$fU_2 = g \tan \gamma_2$$

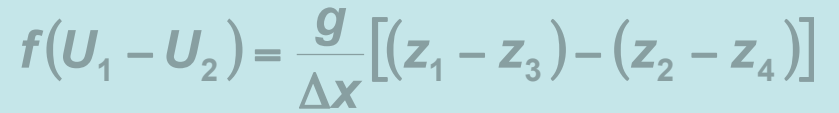
$$f(U_1 - U_2) = g(\tan \gamma_1 - \tan \gamma_2)$$

$$f(U_1 - U_2) = \frac{g}{\Delta x} [B_1 B_2 - A_1 A_2]$$

$$f(U_1 - U_2) = \frac{g}{\Delta x} [(z_1 - z_3) - (z_2 - z_4)]$$

de la ecuación hidrostática : $g dz = -\alpha dp$

$$\int_{B_1}^{B_2} g dz = g(z_3 - z_1) = - \int_{P_1}^{P_2} \alpha_B dp = - \int_{P_1}^{P_2} \alpha_{35,0,p} dp - \int_{P_1}^{P_2} \delta_B dp$$



$$\int_{A_1}^{A_2} g dz = g(z_4 - z_2) = - \int_{P_1}^{P_2} \alpha_{35,0,p} dp - \int_{P_1}^{P_2} \delta_A dp$$

$$(U_1 - U_2) = \frac{1}{f \Delta x} \left\{ \int_{P_1}^{P_2} \delta_B dp - \int_{P_1}^{P_2} \delta_A dp \right\}$$

Anomalías de geopotencial

Estación A: 41°55'N, 50°09'W

m²/s²

Estación B: 41°28'N, 50°09'W

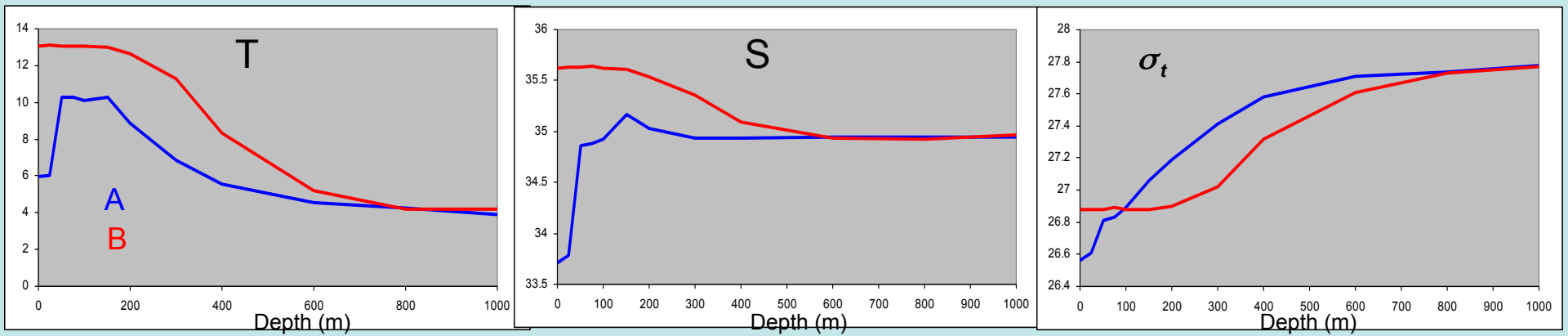
m²/s²

Depth (m)	T°C	S	σ_t kg/m ³	δ_A m ³ /kg	$\bar{\delta}$ X10 ⁻⁸	$\bar{\delta} \times \Delta p$ 10 ⁴ Pa	$\sum \bar{\delta} \times \Delta p$ = $\Delta\Phi_A$
0	5.99	33.71	26.53	148			6.638
25	6.00	33.78	26.61	144	146	0.365	6.273
50	10.30	34.86	26.81	126	135	0.338	5.935
75	10.30	34.88	26.83	125	126	0.315	5.620
100	10.10	34.92	26.89	119	122	0.305	5.315
150	10.25	35.17	27.06	104	112	0.560	4.755
200	8.85	35.03	27.19	93	99	0.455	4.300
300	6.85	34.93	27.41	73	83	0.830	3.470
400	5.55	34.93	27.58	57	65	0.650	2.820
600	4.55	34.95	27.71	46	52	1.040	1.780
800	4.25	34.95	27.74	45	45	0.900	0.880
1000	3.90	34.95	27.78	43	44	0.880	0

Depth (m)	T°C	S	σ_t kg/m ³	δ_B m ³ /kg	$\bar{\delta}$ X10 ⁻⁸	$\bar{\delta} \times \Delta p$ 10 ⁴ Pa	$\sum \bar{\delta} \times \Delta p$ = $\Delta\Phi_B$
0	13.04	35.62	26.88	118			7.894
25	13.09	35.63	26.88	119	119	0.298	7.596
50	13.07	35.63	26.88	119	119	0.298	7.298
75	13.05	35.64	26.89	119	119	0.298	7.000
100	13.05	35.62	26.88	121	120	0.300	6.700
150	13.00	35.61	26.88	122	122	0.610	6.090
200	12.65	35.54	26.90	121	122	0.610	5.480
300	11.30	35.36	27.02	112	117	1.170	4.310
400	8.30	35.09	27.32	83	98	0.980	3.330
600	5.20	34.93	27.61	57	70	1.400	1.930
800	4.20	34.92	27.73	46	52	1.030	0.900
1000	4.20	34.97	27.77	44	45	0.900	0

$\sigma_{35,0,0} = 28.106$

1000 m es el NMV; recordar que 1 db = 10⁴ Pa



Anomalías de geopotencial y la velocidad relativa entre A y B

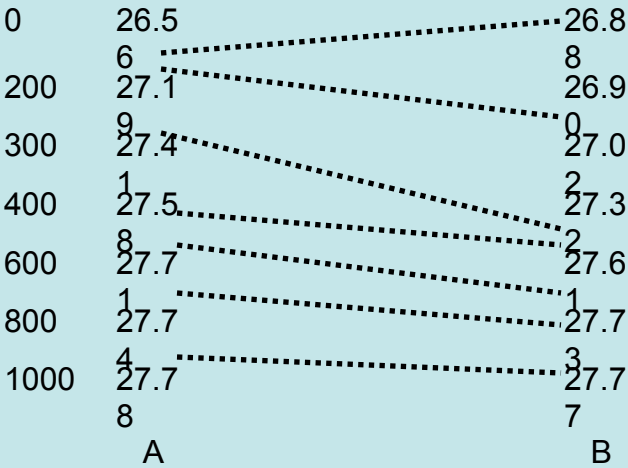
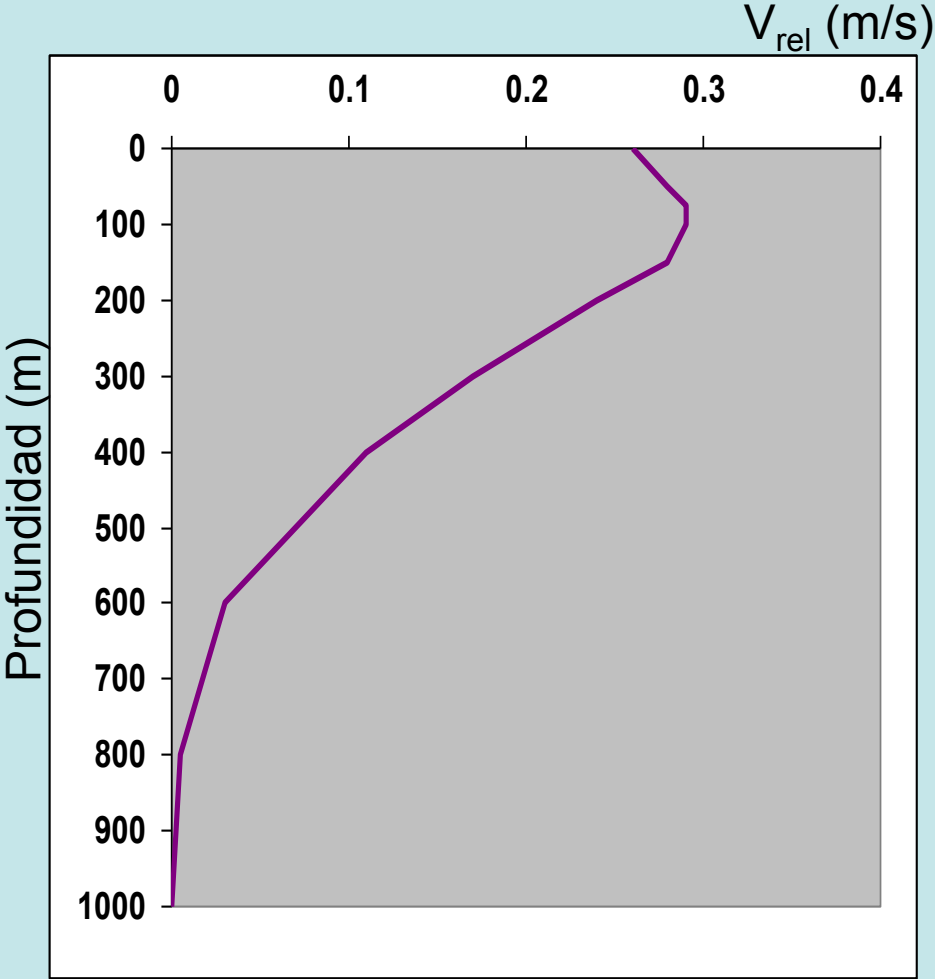
PROF (m)	$\Delta\Phi_B$ m ² /s ²	$\Delta\Phi_A$ m ² /s ²	$\Delta\Phi_B - \Delta\Phi_A$ m ² /s ²	V_{rel} m/s
0	7.894	6.638	1.256	0.26
25	7.596	6.273	1.323	0.27
50	7.298	5.935	1.363	0.28
75	7.000	5.620	1.380	0.29
100	6.700	5.315	1.385	0.29
150	6.090	4.755	1.335	0.28
200	5.480	4.300	1.180	0.24
300	4.310	3.470	0.840	0.17
400	3.330	2.820	0.510	0.11
600	1.930	1.780	0.150	0.03
800	0.900	0.880	0.020	0.005
1000	0	0	0	0

$$(U_1 - U_2) = \frac{1}{f \Delta x} \{ \Delta\Phi_B - \Delta\Phi_A \}$$

$\Delta x = 27'$ o 27 millas náuticas

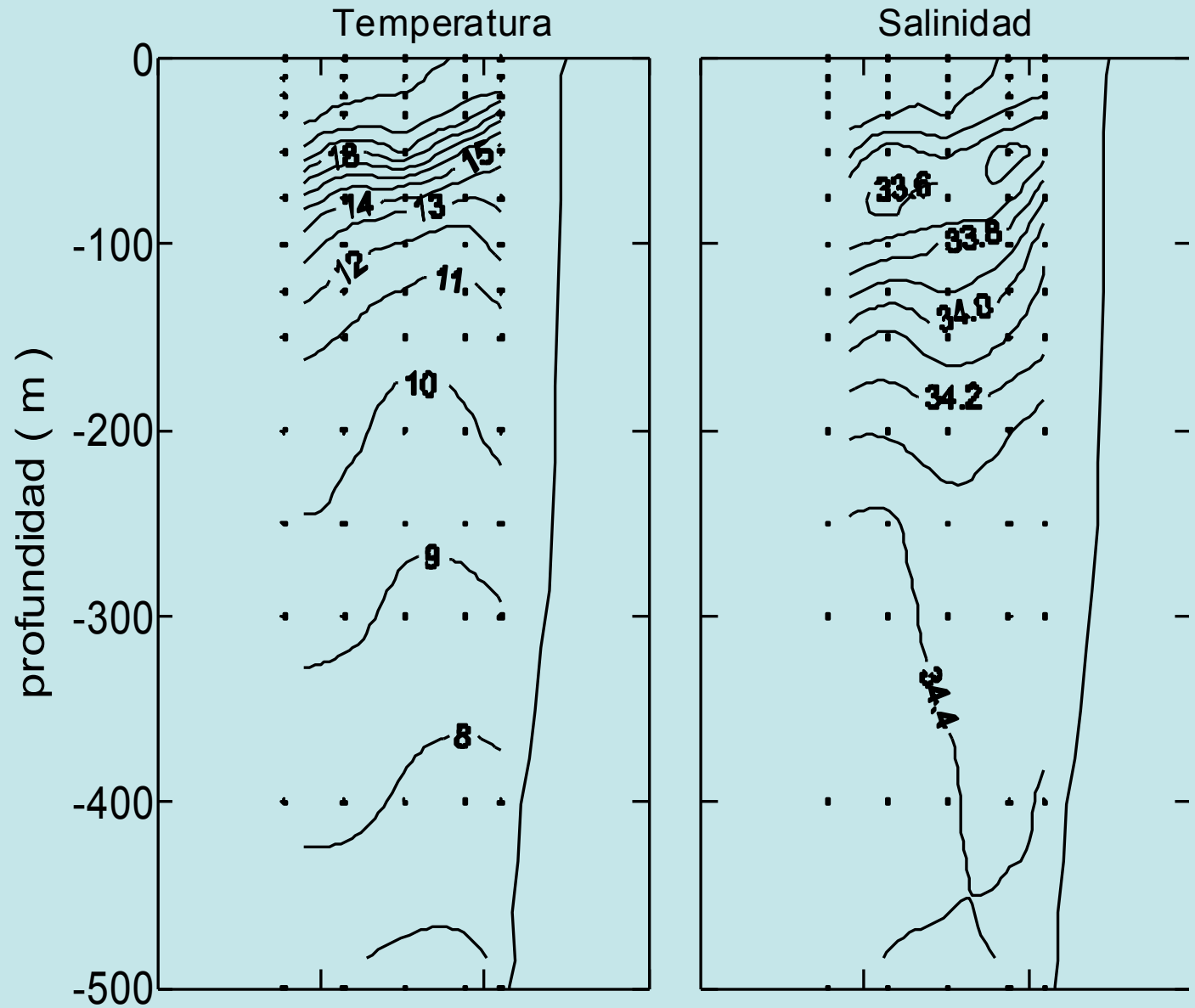
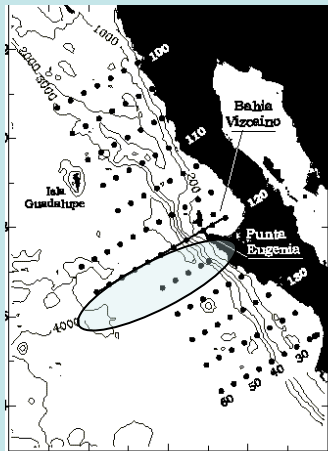
27 m.n. x 1852 m/m.n. = 50,000 m

$f = 9.7 \times 10^{-5} \text{ s}^{-1}$



Seccion 123, crucero 0010

EJEMPLO
IMECOCAL

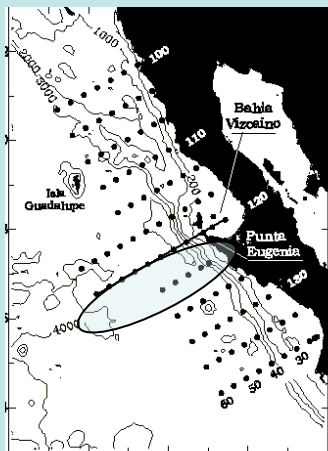
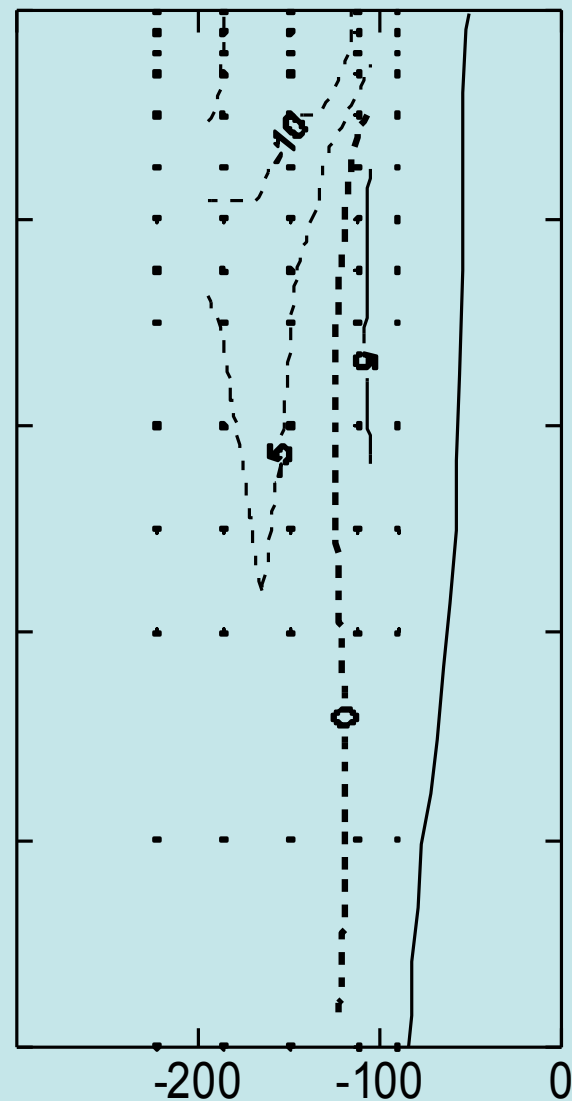
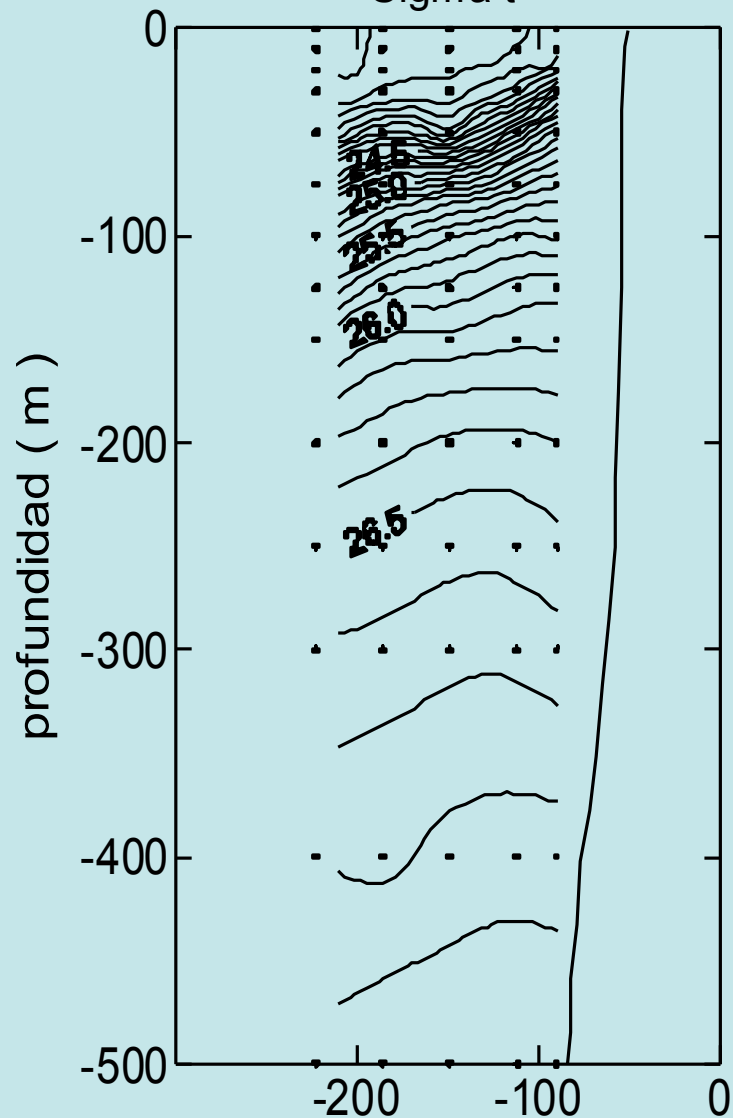


**EJEMPLO
IMECOCAL**

Seccion 123, crucero 0010

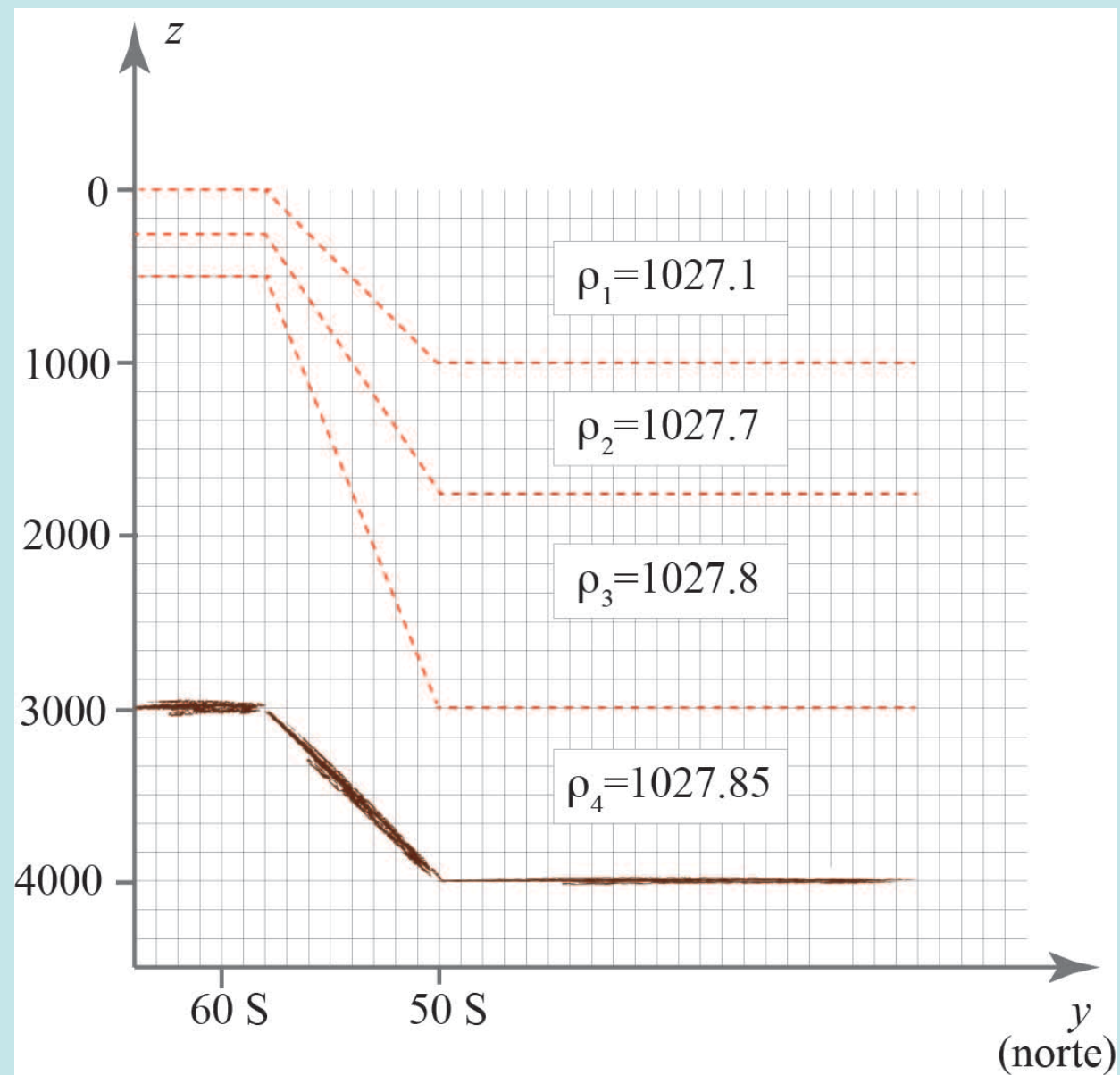
Sigma-t

Vel. Geostrofica



distancia de est. 30 (km)

distancia de est. 30 (km)



$$f(u_1 - u_2) = g'_1 \tan \gamma_1$$

$$f(u_1 - u_2) = g'_1 \tan \gamma_1$$

$$f(u_1 - u_2) = g'_1 \tan \gamma_1$$

$$g'_1 = \frac{\rho_2 - \rho_1}{\rho_1} g$$

$$\tan \gamma = \frac{\Delta z}{\Delta y}$$